

Spacecraft and Aircraft Dynamics

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Lecture 8: Roll Control and Review

In this Lecture we will cover:

Roll Stability

- Contributions to Rolling Moment
- Aileron Control

Review

- A Short Review of Static Stability Equations
- A Summary of Coefficients

Axial Stability

Stability in the y-z plane

We cannot discuss rolling motion without pitch and yaw. Why?

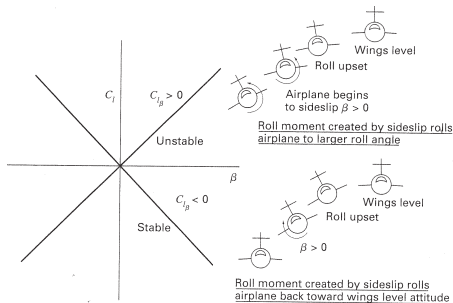
To define the EOM, $I\ddot{\phi} = C_l(\phi)$, we want

$$C_l = C_{l0} + C_{l\phi}\phi$$

However, if $\beta = 0$ and $\alpha = 0$, then the velocity vector \vec{V} does not change with ϕ . If we only count aerodynamic forces, then this means

$$C_{l\phi} = 0$$

This means **ANY** ϕ is a neutrally stable equilibrium.



Axial Stability

Coupling with sideslip

To be useful, we bend our definition of static stability even further.

Consider the rolling angle coupled with motion in the y -direction. For a positive ϕ , the Lift vector becomes

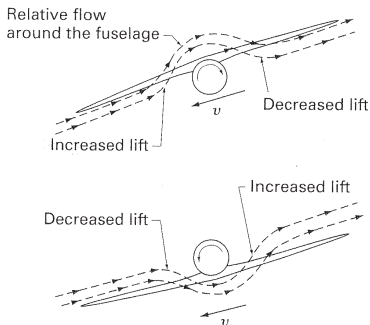
$$\vec{F} = \begin{bmatrix} 0 \\ L \sin \phi \\ -L \cos \phi \end{bmatrix} \cong \begin{bmatrix} 0 \\ L\phi \\ -L \end{bmatrix}$$

In a pseudo-static world, suppose that V_y is proportional to $L\phi$. Specifically, let

$$V_y \cong K\phi$$

This creates a proportional relationship between roll angle and sideslip, angle

$$\beta \cong \frac{V_y}{V} \quad \text{hence} \quad \beta \cong \frac{K}{V}\phi$$



Axial Stability

Coupling with sideslip

The horizontal motion creates aerodynamic roll moments proportional to ϕ .

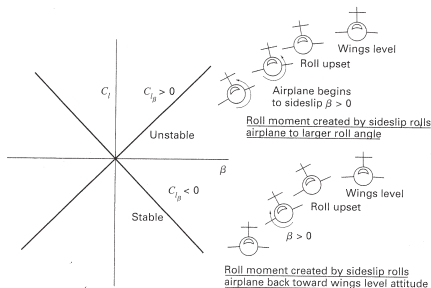
$$C_l = \frac{dC_l}{d\phi} \phi = \frac{dC_l}{d\beta} \frac{d\beta}{d\phi} \phi = C_{l\beta} \frac{K}{V} \phi$$

We write the equations of motion for ϕ .

$$I\ddot{\phi} = QScC_l = \frac{QScK}{V} C_{l\beta} \phi$$

Since Q , S , c , K and V are all positive:
The aircraft is

- Axial **Stable** if $C_{l\beta} < 0$
- Axial **Unstable** if $C_{l\beta} > 0$



Rolling Moment

Moment Contributions

A horizontal velocity, V_y creates two primary sources of rolling moment:

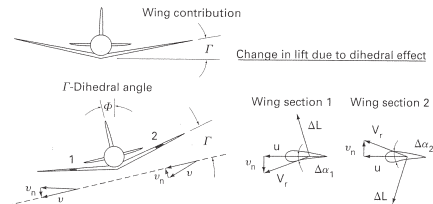


Figure: Wing Dihedral: Positive Roll, Front View

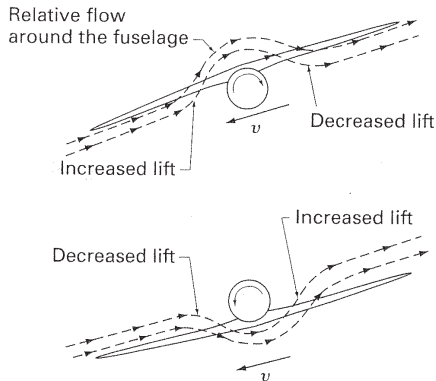


Figure: Fuselage Interaction: Positive Roll, Front View

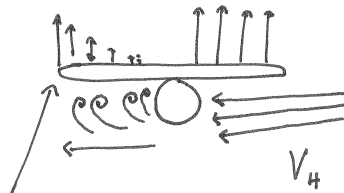
Rolling Moment

Fuselage interaction

The wing acts as a lifting surface with $Q = \frac{1}{2}\rho V_y^2$ and $\alpha = -\phi$. Consider top-mounted wings

- A negative roll creates a positive V_y
- The fuselage blocks the free-stream V_y , reducing the velocity at the downstream wing.
- This reduces the dynamic pressure on the bottom of the downstream wing, Q_d , reducing the lift as $L_d = C_{L\alpha}\phi Q_d S$.
- A moment differential between the wings is created

$$C_l = C_{L\alpha} l_{ac} S (Q_d - Q_u) \phi$$



Reduced Lift

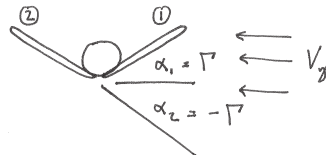
Figure: Fuselage Interaction:
Negative Roll, Front View

Mounting wings on the bottom will create the **Opposite** effect!

Rolling Moment

Wing Dihedral

- A negative roll creates a positive V_y
- With respect to V_y , upstream wing has positive AOA, Γ ; downstream wing has negative AOA, $-\Gamma$.
- This creates positive lift differential on upstream wing and negative lift downstream.
- A positive moment differential between the wings is created.



$$L_1 = C_{L\alpha} \Gamma$$

$$L_2 = -C_{L\alpha} \Gamma$$

Figure: Wing Dihedral: Negative Roll, Front View

$$C_{l0} = 2C_{L\alpha}l_{ac}SQ\Gamma$$

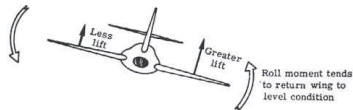
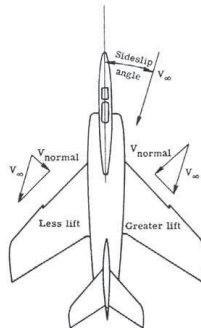
Other Contributions

Wing Sweep

Wing sweep creates roll stability

- A positive roll creates a positive β .
- A Positive β means a negative Yaw (ψ).
- A negative ψ creates a larger V_{\perp} on the right wing.
- A larger V_{\perp} means more lift.
- The right wing rotates up, reducing ϕ

A result of coupling between y , ψ , and ϕ



Other Contributions

Tail

The same **Force** as for directional stability, different moment arm

- A positive roll creates a positive β .
- Sideslip creates pressure on tail surface.
- Pressure on tail creates positive Rotation.

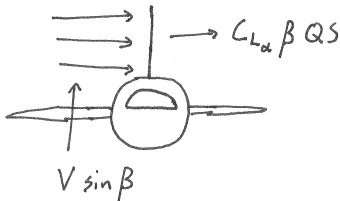


Figure: Roll Stability

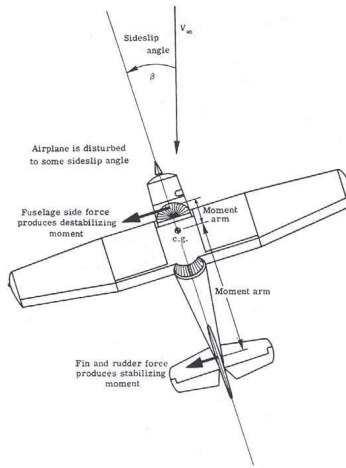


Figure: Directional Stability

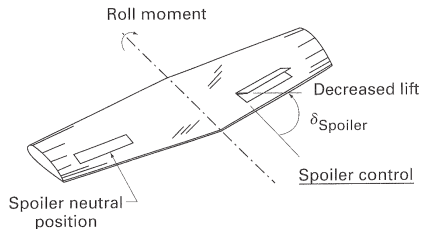
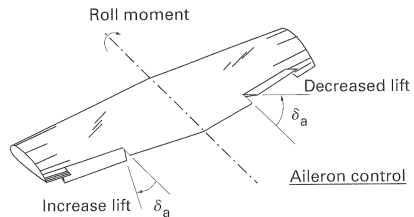
Roll Control

Ailerons

Ailerons are control surfaces attached to the wings. They are similar to elevators, but move in opposite directions.

A δ_a is defined as

- A downwards deflection on the left.
- An upwards deflection on the right.



Roll Control

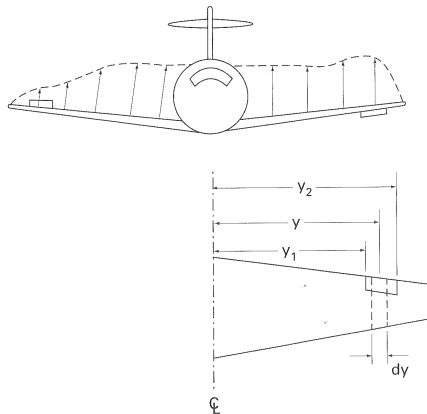
Ailerons

The change in lift on the right wing is

$$\Delta C_{L\alpha} = -\tau_a C_{L\alpha} \delta_a$$

The change in lift on the left wing is positive. The overall moment contribution is described as

$$C_l = C_{l\beta}\beta + C_{l\delta_a}\delta_a$$



$$C_{l\delta_a} = 2 \frac{C_{L\alpha} \tau}{Sb} \int_{y_1}^{y_2} c y dy \cong 2 C_{L\alpha} \tau \frac{y_c}{b}$$

Directional Stability

Example: Cessna Skyhawk

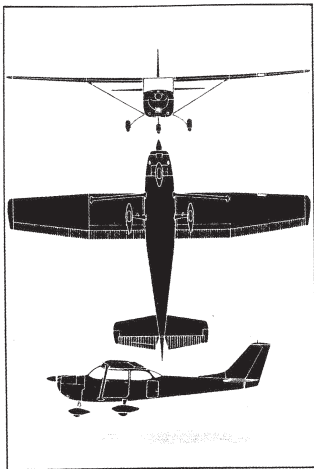
© 1987 Cessna Aircraft Company



Cessna Model 172 Skyhawk USA

Type: light sports aircraft

Accommodation: two pilots, two passengers



Dimensions:

Length: 26 ft 11 in (8.2 m)

Wingspan: 35 ft 10 in

(10.9 m)

Height: 8 ft 9 in (2.7 m)

Weights:

Empty: 1433 lb (650 kg)

Max T/O: 2400 lb (1089 kg)

Payload: 120 lb (54 kg)

Performance:

Max speed: 141 mph

(228 km/h)

Range: 875 nm (1620 km)

Power plant: one Avco

Lycoming O-320-D2J piston engine

Thrust: 160 hp (119 kW)

Variants:

T-41 Mescalero; floatplane;

FR 172K armed version

Notes: One of the most popular light aircraft ever, some 35 545 examples have been built, including the Reims F172 built in France.

Roll Stability

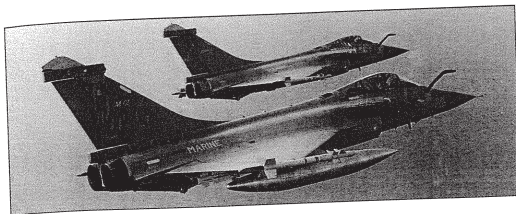
Example: Dassault Rafale

Dassault Rafale France



Type: multi-purpose fighter

Accommodation: one pilot



Dimensions:

Length: 50 ft 2 in (15.30 m)
Wingspan: 35 ft 9 in (10.9 m)
Height: 17 ft 6 in (5.34 m)

Weights:

Empty: 19 973 lb (9060 kg);
21 319 lb (9800 kg) Rafale M
Max T/O: 47 399 lb (21 500 kg)

Performance:

Max Speed: Mach 2

Range: 2000 nm (3706 km)
air-to-air; 1180 nm (2186 km)
ground attack
Powerplant: two SNECMA
M88-2 augmented turbopfans
Thrust: 21 900 lb (97.4 kN) -
32 800 lb (145.8 kN) with
afterburner

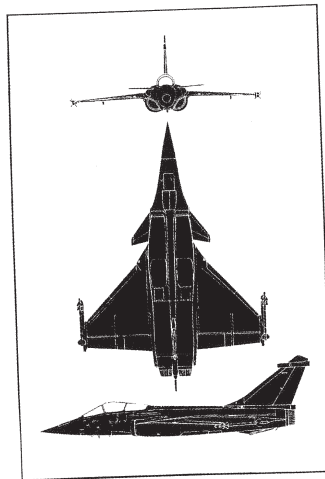
Armament:

one 30 mm DEFA 791B
cannon; Maximum of 14

hardpoints; 13 228 lb (6000
kg) warload; ASMP stand-off
nuclear weapon; Mica AAMs;
Apache stand-off weapon
dispenser; Exocet ASMs; bombs

Variants:

Rafale A proof of concept
demonstrator; Rafale B two-
seat operational trainer;
Rafale C for French Air Force;
Rafale M carrier borne fighter



Notes: 250 planned for French Air Force and 86 for French Navy. In an attempt to replace the ageing F-8 Crusader as soon as possible, the first naval aircraft will lack the full avionics suite to bring them into service earlier.

Directional Stability

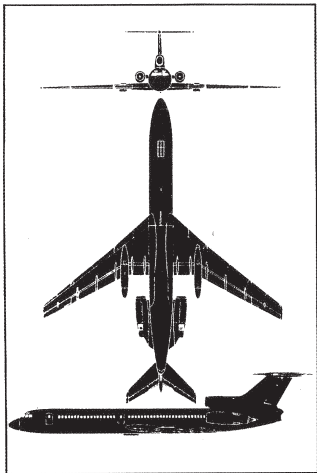
Example: Tu-154



Tupolev Tu-154 Careless Russia

Type: medium-haul airliner

Accommodation: two pilots; flight engineer; optional navigator; 167 passengers



Dimensions:

Length: 157 ft 1 in (47.9 m)

Wingspan: 123 ft 2 in
(87.5 m)

Height: 37 ft 4 in (11.4 m)

Weights:

Empty: 95 900 lb (43 500 kg)

Max T/O: 198 416 lb

(90 000 kg)

Payload: 44 090 lb

(20 000 kg)

Performance:

Cruising speed: Mach 0.9

Range: 2850 nm (5280 km)

Power plant: three Kuznetsov

NK-8-2 turbofans

Thrust: 62 850 lb (279.9 kN)

Variants:

154A, 154B developed versions; 154C cargo; 154M reduced size and redesigned tailplane

Notes: First flown in 1968, the Tu-154 was designed to cover the medium stages of Aeroflot's internal routes. To carry out these duties it can operate from low-grade airfields including packed earth and gravel.

Directional Stability

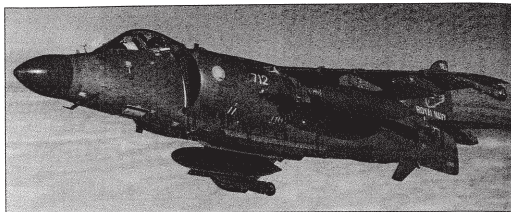
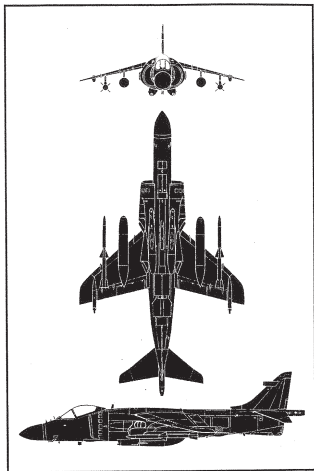
Example: Harrier



BAe Sea Harrier F/A Mk 2 UK

Type: carrier borne multi-role fighter

Accommodation: one pilot



Dimensions:

Length: 46 ft 6 in (14.17 m)
Wingspan: 25 ft 3 in (7.70 m)
Height: 12 ft 2 in (3.71 m)

Weights:

Empty: 14 052 lb (6374 kg)
Max T/O: 26 200 lb (11 880 kg)

Performance:

Max Speed: Mach 1.25; 736 mph (1185 km/h) low level
Range: 800 nm (1500 km)
Powerplant: one Rolls-Royce Pegasus Mk106 vectored Thrust turbofan
Thrust: 21 500 lb (95.6 kN)

Armament:

two 30 mm ADEN cannon pods; five hardpoints; 8000 lb (3630 kg) warload - 5000 lb (2270 kg) with vertical take off; AMRAAM/AIM-7M Sidewinder AAMs; Sea Eagle SSMs; WE117 nuclear bomb; bombs; rockets

Notes: Essentially a stretched Sea Harrier FRS Mk 1 with new radar and avionics, plus the ability to carry the AIM-120 AMRAAM (the first European fighter so equipped), the F/A Mk 2 has now virtually replaced its predecessor in squadron service in the Royal Navy's Fleet Air Arm.

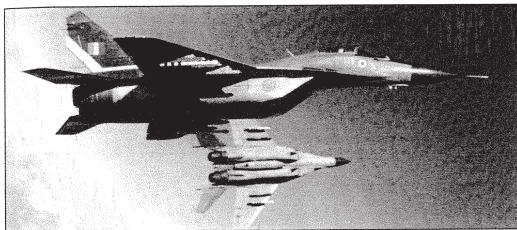
Directional Stability

Example: Mig 29

Mikoyan MiG-29 Fulcrum Russia

Type: multi-role fighter

Accommodation: one pilot



Dimensions:

Length: 48 ft 9 in (14.87 m)
Wingspan: 37 ft 3 in (11.36 m)
Height: 15 ft 6 in (4.73 m)

Weights:

Empty: 24 030 lb (10 900 kg)
Max T/O: 40 785 lb (18 500 kg)

Performance:

Max Speed: Mach 2.3
Range: 1133 nm (2100 km)
Powerplant: two
Klimov/Sarkisov RD-33
turbofans
Thrust: 22 220 lb (98.8 kN)

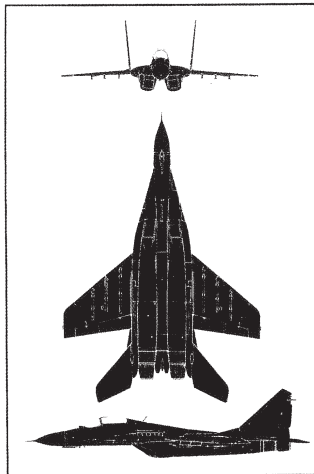
Armament:

one 30 mm GSh-301 cannon;
seven hardpoints; R-77, R-60MK, R-27R1, AAMs; weapons
dispensers; bombs; rockets

Variants:

MiG-29UB trainer; MiG-29K
carrier borne fighter

Notes: The 'Fulcrum-C' and MiG-29S have a larger curved spine housing an active jammer and fuel. MiG-29M with FBW controls, sharp LERX, new spine, broad-chord tailplanes and PGM capability. The MiG-29K did extensive trials aboard the aircraft carrier Kuznetsov.



Directional Stability

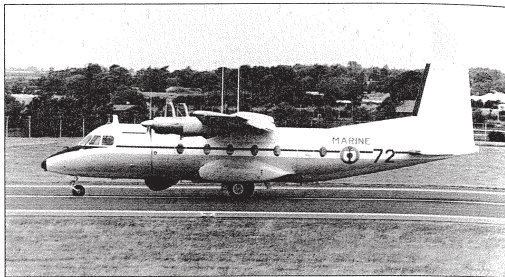
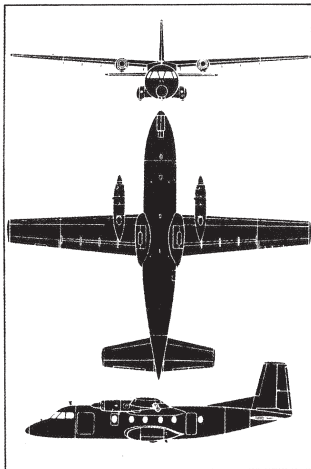
Example: Frégate



Aerospatiale N 262 Frégate France

Type: light military transport

Accommodation: two pilots; 29 troops; 18 paratroops



Dimensions:

Length: 63ft 2in (19.2m)

Wingspan: 71ft 8in (21.9m)

Height: 20ft 4in (6.2m)

Weights:

Empty: 6175lb (13 613kg)

Max T/O: 23 370lb (10 600kg)

Payload: 6834lb (3100kg)

Performance:

Max Speed: 260mph
(418km/h)

Range: 1295nm (1490km);
565nm (650km) with Max
payload

Powerplant: two Turbomeca
Bastan VIIA turboprops
Thrust: 2260ehp (1685.2KW)

Variants:

short-haul civil commuter

Notes: The French Air Force still operates the Frégate in a utility transport and training role, the civil version is rare.

Directional Stability

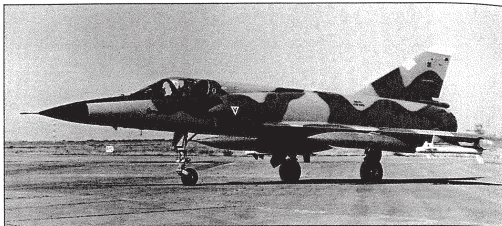
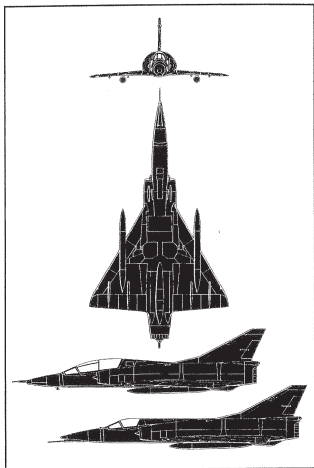
Example: Mirage



Dassault Mirage 50 France

Type: multi-role fighter

Accommodation: one pilot



Dimensions:

Length: 51 ft (15.56 m)
Wingspan: 26 ft 11 in (8.22 m)
Height: 14 ft 9 in (4.5 m)

Weights:

Empty: 15 765 lb (7150 kg)
Max T/O: 30 200 lb (13 700 kg)

Performance:

Max Speed: Mach 2.2
Range: 1330 nm (2410 km);
740 nm (1370 km) low level
Powerplant: one SNECMA
Atar 9K-50 turbojet
Thrust: 15 873 lb (70.6 kN)
with afterburner

Armament:

two 30 mm DEFA cannon;
seven hardpoints; Matra
R.530, Magic, AIM-9
Sidewinder AAMs; Exocet,
AS.30 ASM; bombs; rockets

Variants:

operational trainer; Pantera (IAI
upgrade of Chilean Mirage 50)

Notes: Re-engined Mirage 5 with additional fuel and a higher payload, Mirage 50s can be equipped with Agave radar and Exocet missile. Both Dassault and IAI are offering upgrades, the latter product featuring a Kfir-style nose plug, whilst the former boasts a Mirage F1-type IFR probe.

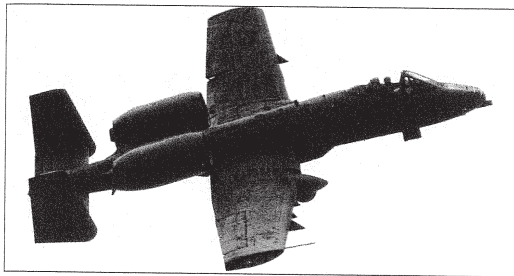
Directional Stability

Example: A10

Fairchild A-10A Thunderbolt USA

Type: close support aircraft

Accommodation: one pilot



Dimensions:

Length: 53 ft 4 in (16.26 m)
Wingspan: 57 ft 6 in (17.53 m)
Height: 14 ft 8 in (4.47 m)

Weights:

Empty: 23 370 lb (10 710 kg)
Max T/O: 47 400 lb (21 500 kg)

Performance:

Max Speed: 449 mph (722 km/h)
Range: 1080 nm (2000 km)
Powerplant: two General Electric TF34-GE-100 high bypass ratio turbofans
Thrust: 18 130 lb (80.6 kN)

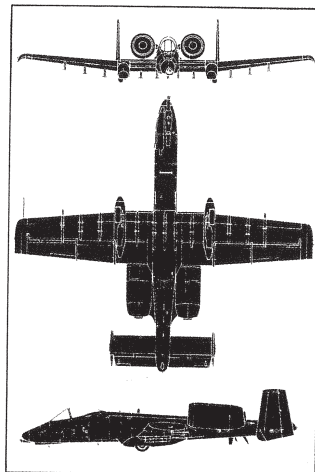
Armament:

one 30 mm GAU-8/A seven-barrelled cannon; 11 hardpoints; 16 000 lb (7257 kg) warload; AGM-65A Maverick; wide range of bombs

Variants:

OA-10A Fast FAC aircraft

Notes: The pilot is protected by a titanium 'bathtub' capable of withstanding 23 mm gun fire.



Directional Stability

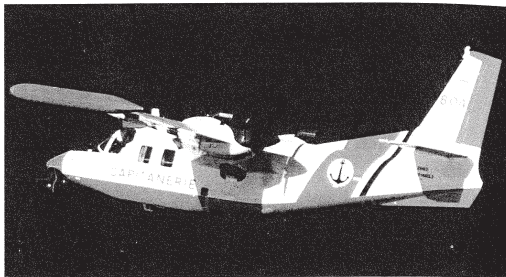
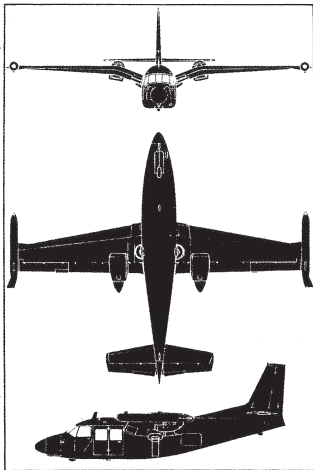
Example: P.166



Piaggio P.166-DL3SEM Italy

Type: offshore patrol aircraft

Accommodation: two pilots plus mission crew



Dimensions:

Length: 39ft (11.8m)
Wingspan: 48ft 2in (14.6m)
Height: 16ft 5in (5m)

Weights:

Empty: 5926lb (2688kg)
Max T/O: 9480lb (4300kg)

Performance:

Max Speed: 248mph
(400km/h)
Range: 1150nm (2130km)
Powerplant: two Lycoming
LTP 101-700 turboprops
Thrust: 1200shp (895kW)

Armament:

no fitted armament

Variants:

special patrol/observation and
transport versions offered

Notes: Used by the Italian Custom Service, Navy, Air Force and Ministry of Merchant Marine.

Roll Instability with Inertia

Falling Leaf Mode

If we truly couple the dynamics of horizontal motion with roll moment, we get

$$\begin{bmatrix} \ddot{y} \\ \ddot{\phi} \end{bmatrix} = K \begin{bmatrix} y \\ \phi \end{bmatrix}$$

When an eigenvalue of K has positive real part, we get motion akin to the “falling leaf” mode, which was unstable in the F/A-18.

This mode will **NOT** be present in static stability dynamics

Falling Leaf Mode

Example: Elevator-Induced

Falling Leaf Mode

Example: F/A-18 Cockpit Camera

Conclusion

We need 6DOF

The dynamics of aircraft are described by 6 degrees of freedom:

Rotational Coordinates

- Roll
- Pitch
- Yaw

Translational Coordinates

- Nose
- Right
- Down

Because body-fixed coordinates are defined in terms of rotation angles, equations for rotational and translational motion cannot be decoupled for aircraft.

In this Lecture, you learned:

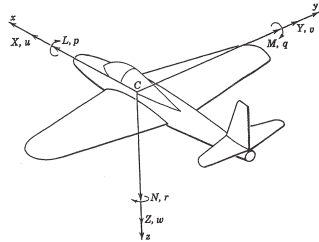
Roll Stability

- Contributions to Roll Stability or instability.
 - ▶ Roll Contributions result from coupling with ψ .
 - ▶ Not really static Stability.
- Control Surfaces.
- A design example.
- Motivation for 6DOF analysis.

Review: Static Stability

Coordinates

- The origin is the center of mass.
- The x -axis points toward the front of the aircraft.
- The z -axis points down.
- The y -axis is perpendicular to the $x - z$ plane.
- Use the “right-hand rule” to define y



Review: Static Stability

Longitudinal Stability

Moment Equation:

$$C_m = C_{m0} + C_{m\alpha}\alpha + C_{m\delta_e}$$

Expressions for $C_{m\alpha}$ and $C_{m\delta}$

$$C_{M0,wf} + \eta V_H C_{L\alpha,t} (\varepsilon_0 + i_{wf} - i_t)$$

$$C_{m\alpha} = C_{L\alpha,wf} \left(\frac{X_{CG}}{\bar{c}} - \frac{X_{AC,wf}}{\bar{c}} \right) - \eta V_H C_{L\alpha,t} \left(1 - \frac{d\varepsilon}{d\alpha} \right)$$

$$C_{m\delta_e} = -\eta V_H C_{L\alpha,t} \tau$$

- Stable if $C_{m\alpha} < 0$
- $\alpha_{eq} = -\frac{C_{m0}}{C_{m\alpha}}$
- Neutral point when $C_{m\alpha} = 0$

Review: Static Stability

Directional Stability

$$C_n = C_{n\beta}\beta + C_{n\delta_r}\delta_r$$

where

$$C_{n\delta_r} = -\eta_v V_v C_{L\alpha, v} \tau,$$

- Stable if $C_{n\beta} > 0$
- Use plots/data to find $C_{n\beta}$

Review: Static Stability

Roll Stability

$$C_l = C_{l\beta}\beta + C_{l\delta_a}\delta_a$$

where

$$C_{l\delta_a} \cong 2C_{L\alpha}\tau\frac{y_c}{b}$$

- Stable if $C_{l\beta} < 0$
- Use plots/data to find $C_{l\beta}$